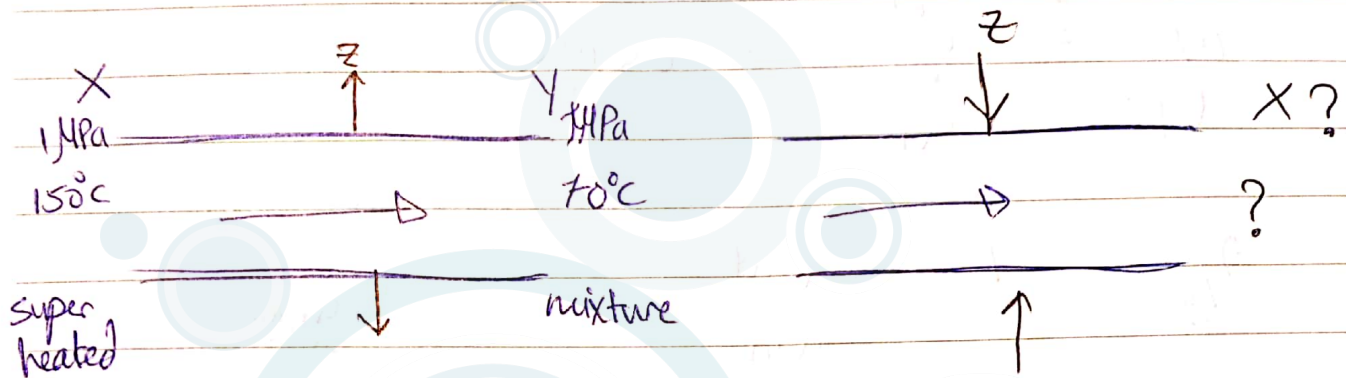


Ch: 7) second law of thermodynamics

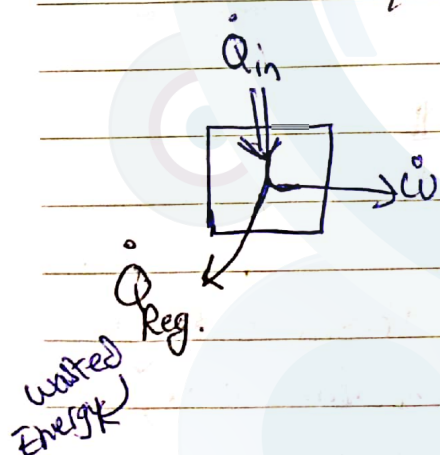


reversible process $\rightarrow$ ideal process
 irreversible process $\rightarrow$ actual process

depends on the path $\rightarrow$ 2nd law $\rightarrow$ manage paths of Energy

focuses on Lost Energy $\rightarrow$ friction
 $\rightarrow$ Q_{loss}

Heat Engine: any device you give it Energy & it gives you work.



you can't take work if and only if you get rejection of heat.

$\dot{Q}_{in} \neq \dot{W}$ impossible

$$\dot{W} = \dot{Q}_{in} - \dot{Q}_{out} \quad (KJ)$$

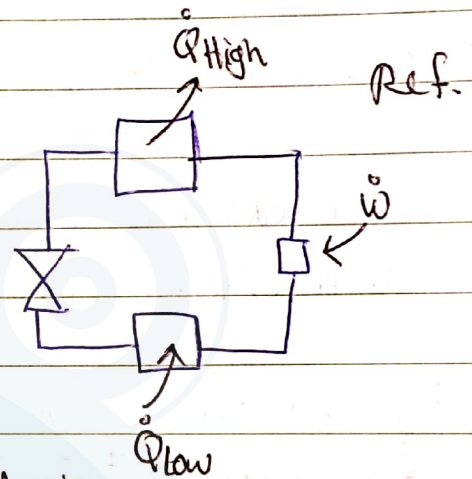
Thermal efficiency :-

$$\eta_{th} = \frac{\dot{W}}{\dot{Q}_{in}} ; 0 < \eta < 1$$

$$\eta_{th} = 1 - \frac{\dot{Q}_{out}}{\dot{Q}_{in}}$$

low $\xrightarrow{\text{external work}}$ High

One path for Energy



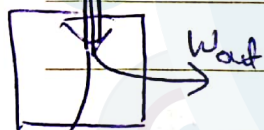
positive

Q_H : magnitude of Q between cyclic device and the high temp. medium at T_H

Q_L : magnitude of Q between cyclic device and the low temp. medium at T_L

$\dot{Q}_{in}/\dot{Q}_H$

$$\dot{W}_{net,out} = \dot{Q}_H - \dot{Q}_L$$



$$\eta_{th} = \frac{W_{out}}{\dot{Q}_H} = 1 - \frac{\dot{Q}_L}{\dot{Q}_H}$$

* Heat is always transferred from a high temp. medium to a low temp. medium one, and never the another way.

→ there will always be Waste Energy

Example 7-1) Net power Production of a Heat Engine

$$\dot{Q}_{in} = P = 20 \text{ MW}$$

$$\dot{Q}_{out} = 50 \text{ MW}$$

① $\dot{W}_{out} = ?$

② $\eta_{th} = ?$

$$\dot{W}_{out} = 20 - 50 = 30 \text{ MW}$$

$$\eta_{th} = \frac{\dot{W}_{out}}{\dot{Q}_{in}} = \frac{30}{20} = 0.375$$

Example 7.2) Fuel consumption Rate of a car

$$\dot{W} = 65 \text{ hp}$$

$$\eta_{th} = 24\%$$

$$\text{Heating value} = 19000 \text{ Btu/lbm}$$

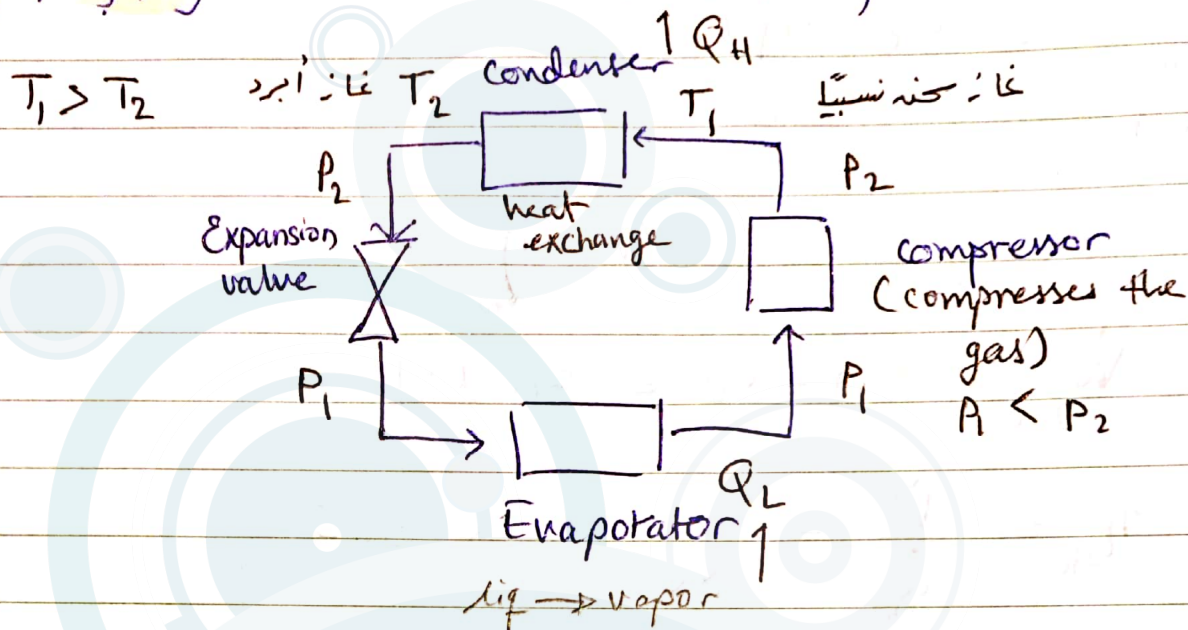
(19000 Btu of Energy is released for each lbm of fuel burned)

rate fuel consumption?

$$\begin{aligned} \dot{Q}_{in} &= \frac{\dot{W}_{out}}{\eta_{th}} = 270.83 \text{ hp} \times \frac{2545 \text{ Btu/h}}{1 \text{ hp}} \\ &= 689262.35 \text{ Btu/h} \end{aligned}$$

$$\dot{m}_{fuel} = \frac{689262.35 \text{ Btu/h}}{1900 \text{ Btu/lbm}} = 36.3 \text{ lbm/h}$$

74 Refrigerator and Heat Pumps



75 Coefficient of performance (COP_R)

The object of a refrigerator is to remove Q_L from the Ref. space.

$$COP_R = \frac{\text{Desired output}}{\text{Required input}} = \frac{Q_L}{W_{in}}$$

$$= \frac{Q_L}{W_{in}} > 1$$

$$= \frac{Q_L}{Q_H - Q_L} = \frac{Q_L}{Q_H - Q_L}$$

$$= \frac{1}{\frac{Q_H}{Q_L} - 1}$$

* Heat pump $\rightarrow$ $\frac{Q_H}{W}$
Desired output $\rightarrow \dot{Q}_H$

$$COP_{HP} = \frac{\dot{Q}_H}{\dot{W}} = \frac{Q_H}{W} = \frac{Q_H}{Q_H - Q_L}$$

$$COP_{HP} = COP_R + 1$$

Ch: 11) Fluid statics

* How we can calculate forces produced by liquids or gases in static

Force $\leftarrow$ pressure $\times$ area

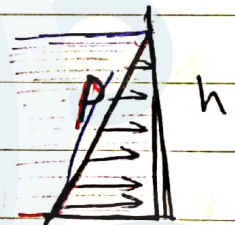
* How we calculate/analyse the stability of the floating submerged bodies (orig)

* Hydrostatic: deals with liquid fluid static

* Aerostatic: deals with gas fluid static

* Hydrostatic $\rightarrow$ Submerged surfaces

$$p = p_{\text{atm}} + \rho g h \quad (\text{open to } p_{\text{atm}}) \quad p \text{ is linearly with } h$$



$$p = p_0 + \rho g h \quad (\text{evaluated or pressurized})$$

$$p_{\text{gage}} = \rho g h = \rho g y \sin \theta$$

For a flat surface (free surface)

$$\textcircled{1} F_R = (p_0 + \rho g y_c \sin \theta) A = (p_0 + \rho g h_c) A = p_{\text{avg}} A_c = p_c A$$

$h_c \rightarrow$ vertical distance to the centroid of area

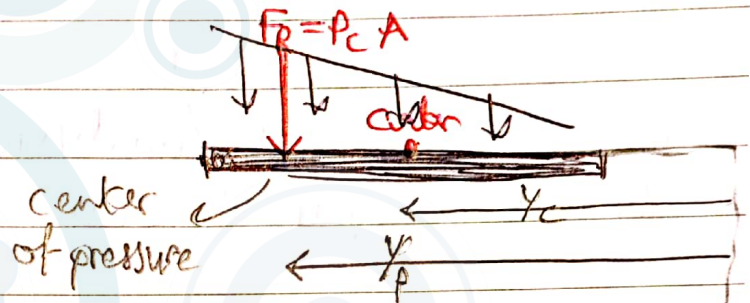
$\downarrow$ centroid of Area

$\downarrow$ center of pressure

* $h_p = y_p \sin \theta$; y_p : vertical distance of the center of pressure from the free surface

location:

$$y_p = y_c + \frac{I_{xxc}}{y_c A}$$



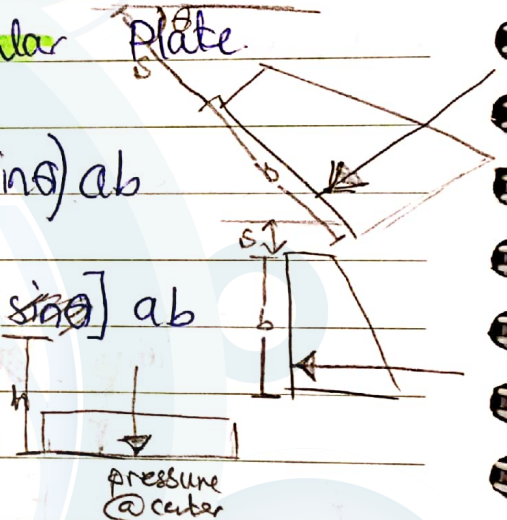
I_{xxc} : moment of Inertia

** Special case: Submerged Rectangular Plate

Inclined plate: $F_R = (P_0 + \rho g (s + b/2) \sin \theta) ab$

Vertical plate: $F_R = [P_0 + \rho g (s + b/2)] ab$

Horizontal plate: $F_R = (P_0 + \rho g h) ab$



location:

$$y_p = s + \frac{b}{2} + \frac{b^2}{12[s + b/2 + P_0/\rho g \sin \theta]}$$

Example 11-1) p: 449

car $\left\{ \begin{array}{l} \text{door} \rightarrow 1.2 \text{ m}, 1 \text{ m} \\ 8 \text{ m below the free surface} \end{array} \right.$

$$\rho_{\text{water}} = 1000 \text{ kg/m}^3$$

① $F_R = ?$ ② $y_p = ?$

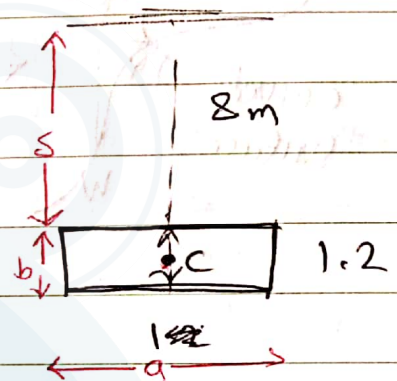
horizontal door $\rightarrow$ vertical Rect. plate

$$F_R = (\rho_0 + \rho g(s + b/2)) ab$$

$$= 1000 \times 9.81 (8 + 0.6) 1.2 (1)$$

$$= 101239.2 \text{ N}$$

$$= 101 \text{ kN}$$



$y_p \rightarrow$ directly under the the midpoint of the door

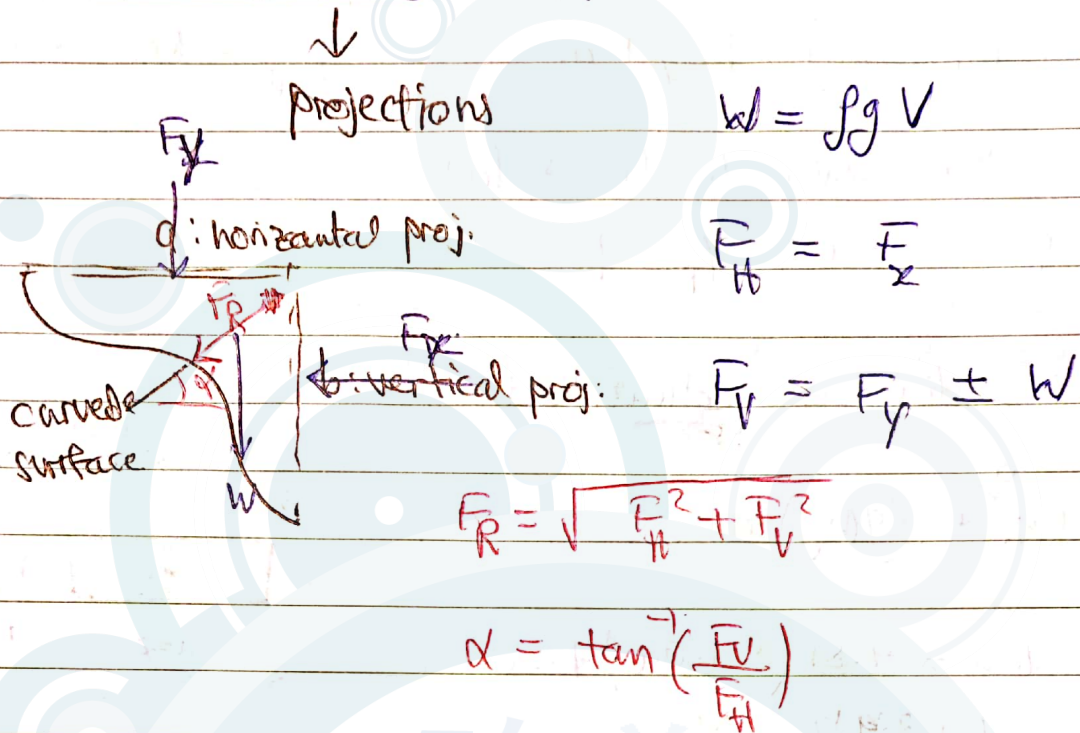
$$y_p = s + \frac{b}{2} = 8 + 0.6 = 8.6 \text{ m}$$

③ (more accurately)

$$y_p = s + \frac{b}{2} + \frac{b^2}{12[s + b/2 + b]} = 8 + 0.6 + \frac{(1.2)^2}{12(8.6)}$$

$$= 8.614 \text{ m}$$

** Curved Surfaces



* multilayered fluid → 2 fluids

differs $\rho \leftarrow$ oil, water
مثال حل

Example 11-2) p145)

$$\textcircled{1} F_H = \rho g h_c A \quad h_c = 5 - 0.8 = 4.6 \text{ m}$$

$$= 1000 \times 9.81 \times 4.6 (0.8 \times 1) = 36.1 \text{ kN}$$

$$\textcircled{2} F_V = F_y - W \quad W = \rho g V$$

$$= 1000 \times 9.81 \times 5(8) - \rho g V$$

$$= 39.2 - 1.3$$

$$= 37.9 \text{ kN}$$

$$= \frac{1000 \times 9.81 \times (R^2 - \frac{R^2}{4})}{1000} = 1.3 \text{ kN}$$

$$\textcircled{3} F_R = \sqrt{37.9^2 + 36.1^2} = 52.3 \text{ kN}$$

$$\tan \theta \Rightarrow \theta = \tan^{-1} \frac{F_V}{F_H} = \theta = 46.4^\circ$$

ch:12) Bernoulli & Energy Equations

Fluid Dynamics $\begin{cases} \text{Bernoulli Equation} \\ \text{Energy Equation} \end{cases}$

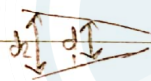
* Bernoulli equation

applies to fluid flow, z, r, ρ



$\rightarrow$ velocity $\rightarrow$ acceleration

$$\frac{\partial d}{\partial t} \rightarrow \frac{\partial v}{\partial t}$$



velocity changes with respect to displacement

$$\frac{\partial v}{\partial d}$$

Steady state flow

$$\frac{\partial}{\partial t} = 0$$

there's no change with time

$$\frac{p_1}{\rho} + \frac{v_1^2}{2} + g z_1 = \frac{p_2}{\rho} + \frac{v_2^2}{2} + g z_2$$

$$p_{\text{static}} + \underbrace{\rho \frac{v^2}{2}}_{\text{Dynamic pressure}} + \underbrace{\rho g z}_{\text{hydrostatic pressure (depends on the level selected)}} = \text{const.}$$

$$p_{\text{stag}} = p + \rho \frac{v^2}{2} \quad [\text{Stagnation pressure}]$$

$\hookrightarrow$ when $v=0$, p is max.

$$v = \sqrt{\frac{2(p_{\text{stag}} - p)}{\rho}} \quad \rightarrow \quad p = \rho g h = \rho g y \sin \theta$$

fluid velocity

* Energy Equation

$$\frac{p_1}{\rho g} + \frac{V_1^2}{2g} + z_1 + h_{\text{pump}} = \frac{p_2}{\rho g} + \frac{V_2^2}{2g} + z_2 + h_{\text{turbine}} + h_L$$

pump, h_{pump} turbine h_{turbine}
 friction h_L

$$\dot{m} \left(\frac{p_1}{\rho g} + \frac{V_1^2}{2g} + z_1 \right) + \dot{W}_{\text{pump}} = \dot{m} \left(\frac{p_2}{\rho g} + \frac{V_2^2}{2g} + z_2 \right) + \dot{W}_{\text{turbine}} + E_{\text{mach. loss}}$$

(height loss)

$$\dot{W} = h * g * \dot{m}$$

* Kinetic Energy correction factor (α)

$$\frac{\alpha V_1^2}{2} ; \frac{\alpha V_2^2}{2}$$

$$\dot{V} = VA = \text{m/s} * \text{m}^2 = \text{m}^3/\text{s} = \frac{\text{L}}{\text{s}}$$

$$\dot{V} = \frac{V}{\Delta t} = \frac{1}{\text{s}}$$

Ch.14) Internal flow

$$\dot{m} = \int \rho V_{avg} A_c = \int_{A_c} \rho u(r) dA_c$$

$$V_{avg} = \frac{2}{R^2} \int_0^R u(r) r \cdot dr$$

* Laminar & Turbulent Flows

Smooth

fluctuating

$$Re \leq 2300$$

transition

$$Re \geq 4000$$

$$2300 < Re < 4000$$

$$Re = \frac{\rho V_{avg} D}{\mu} = \frac{V_{avg} \cdot D}{\nu} = \frac{\text{Inertial forces}}{\text{Viscous forces}}$$

(Reynolds #)

circular

non circular

D = the same diameter of the cylinder

square

rectangle

$$D_h = \frac{4a^2}{4a} = a$$

$$D_h = \frac{2ab}{a+b}$$

In general: $D_h = \frac{4A_c}{P}$

المساحة
التي
تحتلها

* laminar flow

Velocity
Profile

$$① \quad u(r) = 2 v_{avg} \left(1 - \frac{r^2}{R^2} \right)$$

Variable $\nearrow$
inner radius $\nwarrow$

function

we use it to find v_{avg}

$$= u_{max} \left(1 - \frac{r^2}{R^2} \right)$$

$$② \quad Re = \frac{v_{avg} \cdot D}{\mu} = \frac{\rho}{\mu} v_{avg} \cdot D$$

Friction
factor

$$f = \frac{64}{Re} = \frac{64 \cdot \mu}{v_{avg} \cdot D \cdot \rho}$$

laminar

Head
loss

$$\Delta P h_L = f \frac{L}{2gD} v_{avg}^2$$

Energy eqn

$$= \frac{\Delta P_L}{\rho g}$$

$$\Delta P = \rho g h$$

$$\Delta P_L = \rho g h_L$$

length of the pipe

pressure
loss

$$③ \quad \Delta P_L = f \frac{L}{D} \frac{\rho v_{avg}^2}{2}$$

$$④ \quad v_{avg} = \frac{\Delta P D^2}{32 \mu L}$$

In Horizontal
pipe

$$\dot{V} = v_{avg} A_c = \frac{\Delta P \pi D^4}{128 \mu L}$$

$$⑤ \quad \dot{W}_{pump} = \dot{V} \Delta P_L = \dot{V} \rho g h_L = \dot{m} g h_L$$

** special case = Inclined pipe (effect of gravity) θ

$$V_{avg} =$$

$$\frac{(\Delta P - \rho g L \sin \theta) D^2}{32 \mu L}$$

θ $\nearrow$ +ve $\rightarrow$ uphill
 $\searrow$ -ve $\rightarrow$ downhill

$$\Delta z = z_2 - z_1 = L \sin \theta$$

$$\dot{V} = \frac{(\Delta P - \rho g L \sin \theta) \pi D^2}{128 \mu L}$$

** Flow in Noncircular pipe $\rightarrow D_h = \frac{4 A_c}{P}$
inner Area
inner circumference
a/b $\rightarrow f$
or θ

** check Page 538

* Turbulent Flow

plastic
cast iron
Turbulent

table 14-2 p: 543
roughness

✓ ②

$$f \Rightarrow \frac{1}{\sqrt{f}} \approx -1.8 \log \left[\frac{6.9}{Re} + \left(\frac{\epsilon/D}{3.7} \right)^{1.1} \right]$$

$$h_L = \checkmark$$

$$\Delta P_L = \checkmark$$

④ ✓

⑤ ✓

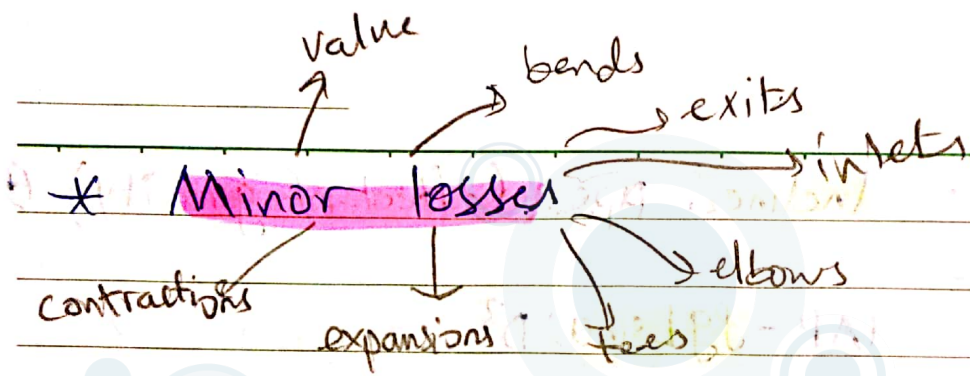
معادلات L و ϵ با هم
میان هم قرار می گیرند

$$h_L = 1.07 \frac{V^2}{g D^5} \left\{ \ln \left(\frac{\epsilon}{3.7 D} + 4.62 \left(\frac{V D}{\dot{V}} \right)^{0.99} \right) \right\}^{-2}$$

$$\dot{V} = -0.965 \left(\frac{g D^5 h_L}{L} \right)^{0.5} \ln \left[\frac{\epsilon}{3.7 D} + \frac{3.7 V^2 L}{g D^5 h_L} \right]^{0.5}$$

check
Page
545

$$D = 0.66 \left[\epsilon^{1.25} \left(\frac{L \dot{V}}{g h_L} \right)^{4.75} + 2 \dot{V}^{9.4} \left(\frac{L}{g h_L} \right)^{5.2} \right]^{0.04}$$



$$h_L = K_L \frac{V^2}{2g} = f \frac{L_{equiv}}{D} \frac{V^2}{2g}$$

$$L_{equiv} = \frac{D}{f} K_L \rightarrow \text{check p: 552}$$

$$h_{L, total} = h_{L, major} + h_{L, minor}$$

laminar
turbulent

$$h_{L, tot.} = \left(f \frac{\sum L}{D} + \sum K_L \right) \frac{V^2}{2g}$$

Heat Transfer

ch:6) mechanism of heat transfer

Conduction

in Solids

gases & liq.

bounded

$$Q_{\text{cond.}} = KA \frac{T_1 - T_2}{\Delta x} \quad (\text{Fourier's law of Heat conduction})$$

$$= -KA \frac{\Delta T}{\Delta x} = -kA \frac{dT}{dx}$$

Thermal conductivity

table 16-1

p: 622

$$\text{Thermal diffusivity} = \alpha = \frac{\text{Heat conduction}}{\text{Heat storage}} = \frac{k}{\rho c_p}$$

قدرة انتقال الحرارة على قدرته، كفاءة تخزين الحرارة

table

16-4

p: 632

convection $\left\{ \begin{array}{l} \text{gas} \\ \text{liq.} \end{array} \right\} \rightarrow \text{motion}$
 solid surface with motionary fluid

velocity vs. $\frac{\text{m}}{\text{s}}$ / $\frac{\text{cm}}{\text{s}}$ $\rightarrow$ $\frac{\text{m}}{\text{s}}$

(free) Natural convection $\rightarrow$
 force convection $\leftarrow$
 Force $\rightarrow$ $\frac{\text{N}}{\text{m}^2}$ / $\frac{\text{kg}}{\text{m}^3}$ / $\frac{\text{m}}{\text{s}^2}$

$Q_{\text{conv}} = h A_s (T_s - T_{\infty})$ [Newton's law of cooling]

Q_{conv} $\rightarrow$ convection coeff
 h $\rightarrow$ surface Area
 A_s $\rightarrow$ surface Area
 T_s $\rightarrow$ fluid
 T_{∞} $\rightarrow$ fluid

Table
 16-5
 p: 635

convection $\rightarrow$ T $\nrightarrow$ K or $^{\circ}\text{C}$
 conduction $\rightarrow$ T $\nrightarrow$ K or $^{\circ}\text{C}$

$W = VI = I Q$

دالة موجية

* **Radiation** (electromagnetic waves)

فوتون ←
جسيم

photons

combined heat transfer → Radiation + convection

$$\Rightarrow \dot{Q}_{\text{rad}} = \epsilon \sigma A_s (T_s^4 - T_\infty^4) \quad \text{W}$$

emissivity Stefan-boltzman coeff Kelvin

$$\Rightarrow \dot{Q}_{\text{absorbed}} = \alpha \dot{Q}_{\text{incident}} \quad \text{W}$$

absorptivity

⇒ **combined heat transfer** سريان سائل

$$\dot{Q}_{\text{tot}} = \dot{Q}_{\text{conv}} + \dot{Q}_{\text{rad}}$$

$$= h_{\text{combined}} A_s (T_s - T_\infty) \quad \text{Kelvin}$$

fluid

$$h_{\text{combined}} = h_{\text{conv}} + h_{\text{rad}} = h_{\text{conv}} + \epsilon \sigma (T_s + T_{\text{surr}})(T_s^2 + T_{\text{surr}}^2)$$

ch:17) Steady heat conduction

Thermal
convection
radiation

Resistance

$R_{\text{wall, cond}}$

R_{conv}

R_{rad}

$$R_{\text{cond}} = \frac{L}{KA}$$

$$R_{\text{conv}} = \frac{1}{hA}$$

$$R_{\text{rad}} = \frac{1}{h_{\text{rad}} A_s}$$

$$Q_{\text{cond}} = \frac{T_1 - T_2}{R_{\text{wall}}}$$

$$Q_{\text{conv}} = \frac{T_s - T_{\infty}}{R_{\text{conv}}}$$

$$Q_{\text{rad}} = \frac{T_s - T_{\text{sur}}}{R_{\text{rad}}}$$

$$Q_{\text{tot}} = h_{\text{combined}} A_s (T_s - T_{\infty})$$

On Series $\rightarrow R_{\text{tot}} = R_1 + R_2 + \dots$

$$Q = \frac{T_{\infty 1} - T_{\infty 2}}{R_{\text{tot}}} = U A \Delta T$$

over
all
heat
transfer

on Parallel $\rightarrow R_{tot} \rightarrow \frac{1}{R_{tot}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$

$$R_{tot} = \frac{R_1 R_2}{R_1 + R_2}$$

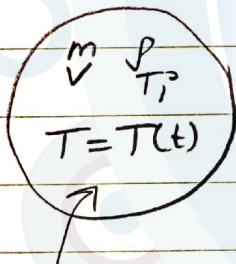
$$\dot{Q} = \frac{T_{w1} - T_{w2}}{R_{tot}}$$

Ch: 8) Transient Heat Conduction

(lumped system analysis)

One unit

single temp.



$$\dot{Q} = h A_s (T_{\infty} - T(t))$$

$$\frac{T(t) - T_{\infty}}{T_i - T_{\infty}} = e^{-bt}$$

$$b = \frac{h A_s}{\rho V C_p}$$

Volume

exponential relation between temp of the body & surr. temp.

$$* \quad \underset{\text{cooling rate}}{Q(t)} = h A_s (T(t) - T_{\infty})$$

$$* \quad Q = m c_p [T(t) - T_{\infty}]$$

total amount of heat after certain temp.

$$* \quad Q_{\max} = m c_p [T_{\infty} - T_i]$$

biot no.

$$Bi = \frac{h L_c}{k}$$

biot no. $\leftarrow$

$$Bi \leq 0.1$$

$$\text{characteristic length} \leftarrow L_c = \frac{V}{A_s}$$