

University of Jordan
School of Engineering
Electrical Engineering Department

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EE 204
Electrical Engineering Lab

EXPERIMENT 7 REPORT & PRE-LAB
RESONANCE

Section # _____ Group # _____

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EXPERIMENT 7

RESONANCE

Note: Use MATLAB to quickly perform theoretical calculations by defining a vector of frequencies then using array arithmetic.

PROCEDURE A - SERIES RESONANCE

4. What is the equation for the resonant frequency of a series RLC circuit?

..... $f_r = \frac{1}{2\pi\sqrt{LC}}$

5. Use that above equation to find the resonant frequency in this experiment.

..... $f_r = 159/5.5 \text{ Hz}$

6. What is the equation for the quality factor Q , and bandwidth B of a series RLC circuit?

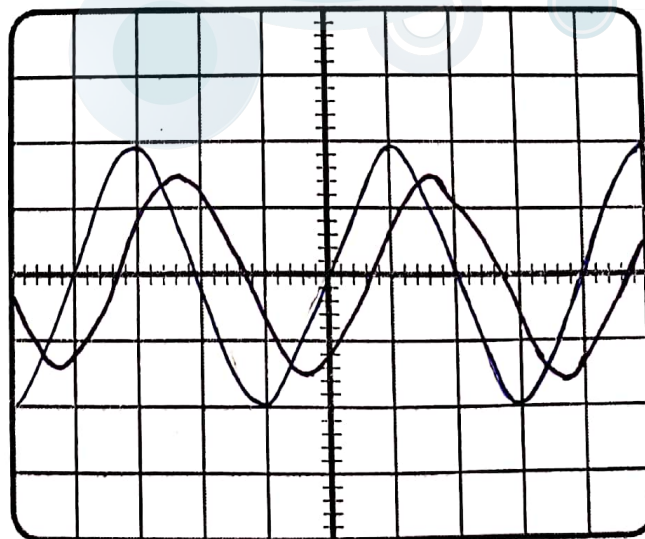
..... $B = \frac{R}{2\pi L}$ $Q = \frac{f_r}{B}$

7. Use the proper equations to find the frequencies f_1 and f_2 , at which the current amplitude is approximately 0.707 times the resonant current (i.e., the half-power points).

..... $f_1 = \left(-\frac{R}{2L} + \sqrt{\left(\frac{R}{2L}\right)^2 + \frac{1}{LC}} \right) / (2\pi)$

..... $f_2 = \left(\frac{R}{2L} + \sqrt{\left(\frac{R}{2L}\right)^2 + \frac{1}{LC}} \right) / (2\pi)$

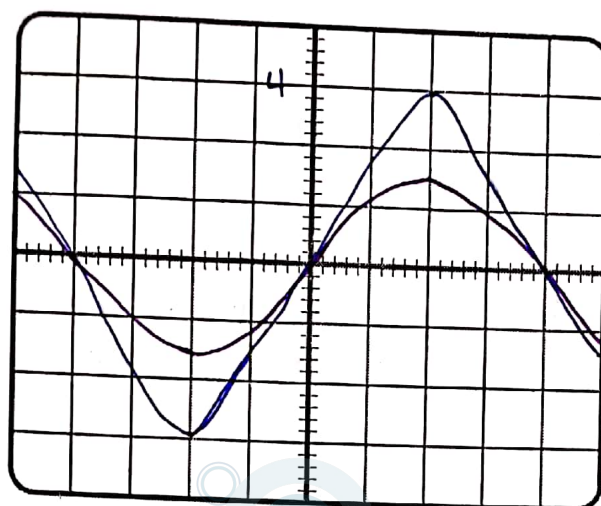
8. At the frequency of 6000 Hz, draw what you see on the oscilloscope screen.



— V_s
— V_R

11. Draw what you see on the oscilloscope screen at the resonant frequency.

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$-V_R$
 $-V_S$
 ~~R~~

Table 1

AC Source Frequency (Hz)	$ V_S $ (peak) (V)		V_S period T (μs)		$ V_R $ (peak) (V)		$\angle V_R$ with V_S (degrees)	
	Theory	Meas.	Theory	Meas.	Theory	Meas.	Theory	Meas.
6000	4	4.03	166.67	169.98	1.356	1.29	70.2°	63.5°
9000	4	4.09	111.11	110.4	2.253	2.11	55.7°	49°
14400	4	4	69.4	69.58	3.886	3.2	13.7°	15.7°
16800	4	4	59.52	59.41	3.966	3.4	-7.5°	-6.4°
30000	4	4	33.33	33.35	2.072	2.3	-58.8°	-50.6°
48000	4	4.09	20.83	20.99	1.169	1.44	-73°	-68.5°
$f_r = 15915$	4	4	62.83	63.37	4	3.35	0°	3°
$f_1 = 10676$	4	4.05	93.67	93.96	2.67	2.3	48.2°	45°
$f_2 = 23727$	4	4.05	42.21	42.33	2.15	2.3	-58.7°	-50°

Table 2

AC Source Frequency (Hz)	$ V_C $ (peak) (V)		$\angle V_C$ with V_S (degrees)		$ V_L $ (peak) (V)		$\angle V_L$ with V_S (degrees)	
	Theory	Meas.	Theory	Meas.	Theory	Meas.	Theory	Meas.
6000	4.386	4.32	-19.8°	-21.17°	0.623	0.6	160.2°	155.4°
9000	4.859	4.52	-34.3°	-37.7°	1.554	1.2	145.7°	143°
14400	5.237	4.41	-76.3°	-77.1°	4.288	3.4	103.7°	102.8°
16800	4.581	4.22	-97.5°	-92.3°	5.105	4.03	82.5°	84°
30000	1.34	1.45	-148.8°	-138.9°	4.762	4.68	31.2°	32°
48000	0.473	0.6	-163°	-171.8°	4.298	4.4	17°	18°
$f_r = 15915$	3.62	3.7	-90°	-90°	4.878	3.4	90°	91.2°
$f_1 = 10676$	5.07	2.48	-41.8°	-45°	2.09	1.8	138.2°	140°
$f_2 = 23727$	1.35	1.65	-148.7°	-142.6°	4.76	4.4	31.3°	35°

16. What is the relationship between the capacitor voltage V_C and inductor voltage V_L at resonant frequency?

..... Equal in magnitude and opposite in direction.....

17. Consider the capacitor voltage amplitude $|V_C|$. Which one is higher $|V_C|$ at resonant frequency or $|V_C|$ below resonant frequency?

... $|V_C|$ below the resonant frequency is higher.....

18. Consider the inductor voltage phase $\angle V_L$. Which one is higher $\angle V_L$ at resonant frequency or $\angle V_L$ below resonant frequency? Note: In phase, consider the positive or negative signs.

... $\angle V_L$ below resonant frequency is higher.....

Table 3

AC Source Frequency (Hz)	$ I $ (peak) (mA) $= V_R/R$		$\angle I$ with V_s $(= \angle V_R \text{ with } V_s)$		$ Z = V_s / I $ (peak/peak) (k Ω)		$\angle Z = \angle V_s - \angle I$ (degrees)	
	Theory	Meas.	Theory	Meas.	Theory	Meas.	Theory	Meas.
6000	1.654	1.573	70.2°	63.5°	2.418	2.562	-70.2°	-63.5°
9000	2.748	2.573	55.7°	49°	1.456	1.589	-55.7°	-49°
14400	4.739	3.902	13.7°	15.7°	0.844	1.025	-13.7°	-15.7°
16800	4.837	4.146	-7.5°	-6.4°	0.827	0.965	7.5°	6.4°
30000	2.527	2.805	-58.8°	-50.6°	1.583	1.426	58.8°	50.6°
48000	1.426	1.756	-73°	-68.5°	2.805	3.329	73°	68.5°
$f_r = 15915$	4.878	4.085	0	3°	0.82	0.979	0	-3°
$f_1 = 10676$	3.256	3.221	48.2°	45°	1.228	1.444	-48.2°	-45°
$f_2 = 23727$	2.622	3.003	-58.7°	-50°	1.526	1.444	58.7°	50°

20. Using the measured values in Table 3, plot (by hand) the following figures using the graph paper attached at the end of the report: (1) $|Z|$ versus source frequency; (2) $\angle Z$ versus source frequency; (3) I versus source frequency.

21. For the above plots, state your conclusions under the plot? Also identify the resonant frequency and bandwidth in each plot.

PROCEDURE B - PARALLEL RESONANCE

4. What is the equation for the resonant frequency of a parallel RLC circuit?

..... $f_r = \frac{1}{2\pi\sqrt{LC}}$

5. Use that above equation to find the resonant frequency in this experiment.

..... 15915.5 Hz.....

6. What is the equation for the quality factor Q , and bandwidth B of a parallel RLC circuit?

..... $Q = \omega_r R C$ $B = \frac{1}{2\pi R C}$

7. Use the proper equations to find the frequencies f_1 and f_2 , at which the current amplitude is approximately $1.414 = 1/0.707$ times the resonant current (i.e., the bandwidth limits).

$$f_1 = \left(-\frac{1}{2RC} + \sqrt{\left(\frac{1}{2RC}\right)^2 + \frac{1}{LC}} \right) / (2\pi)$$

$$f_2 = \left(\frac{1}{2RC} + \sqrt{\left(\frac{1}{2RC}\right)^2 + \frac{1}{LC}} \right) / (2\pi)$$

Table 4

AC Source Frequency (Hz)	V_s (peak) (V)		V_s period T (μs)		$V_{R'}$ (peak) (V)		$\angle V_{R'}$ with V_s (degrees)	
	Theory	Meas.	Theory	Meas.	Theory	Meas.	Theory	Meas.
6000	4	4.05	166.67	166.67	0.102	0.115	-60.5°	-63.8°
9000	4	4.04	111.11	111.9	0.068	0.07	-43.9°	-42.7°
14400	4	4.04	69.4	69.93	0.049	0.052	-9.2°	-12.2°
16800	4	4.03	59.52	59.4	0.048	0.062	5°	15°
30000	4	4.03	33.33	33.48	0.072	0.078	47.2°	42.4°
48000	4	4	20.83	20.81	0.116	0.124	64°	63°
$f_r = 15915$	4	4.03	62.83	64.3	0.048	0.062	0°	2°
$f_1 = 8936.3$	4	4	111.9	111.82	0.067	0.07	-40.2°	-38°
$f_2 = 28345.4$	4	4.03	35.28	35.33	0.07	0.075	47.1°	42.8°

12. What is the relationship between the capacitor current I_C and inductor current I_L at resonant frequency?

..... They are equal

13. Consider the capacitor current phase $\angle I_C$. Which one is higher $\angle I_C$ at resonant frequency or $\angle I_C$ above resonant frequency? Note: In phase, consider the positive or negative signs.

~~At~~ I_C at resonant frequency is higher: ... ($\angle I_C$ & $\angle I_L$)

14. Consider the inductor current amplitude $|I_L|$. Which one is higher $|I_L|$ at resonant frequency or $|I_L|$ above resonant frequency?

..... $|I_L|$ at resonant frequency is higher

$f \uparrow, |X_L| \uparrow, V_{\text{constant}}, |I_L| \downarrow$

AC Source Frequency (Hz)	I (peak) (mA) = $V_{R'}/R'$		$\angle I$ with V_s (= $\angle V_{R'}$ with V_s)		$ Y = I / V_s $ (peak/peak) (mS)		$\angle Y = \angle I - \angle V_s$ (degrees)	
	Theory	Meas.	Theory	Meas.	Theory	Meas.	Theory	Meas.
6000	10.2	11.5	-60.5°	-63.8°	2.55	2.88	-60.5°	-63.8°
9000	6.8	7	-43.9°	-42.7°	1.7	1.75	-43.9°	-42.7°
14400	4.9	5.2	-9.2°	-12.2°	1.23	1.3	-9.2°	-12.2°
16800	4.8	5	5°	15°	1.2	1.27	5°	15°
30000	7.2	7.8	47.2°	42.4°	1.8	1.95	47.2°	42.4°
48000	11.6	12.4	64°	63°	2.9	3.1	64°	63°
$f_r = 15915$	4.8	4.7	0°	2°	1.2	1.25	0°	2°
$f_1 = 8936.3$	6.7	7	-45.2°	-48°	1.67	1.75	-45.2°	-48°
$f_2 = 28345.4$	7.2	7.5	47.1°	42.8°	1.75	1.88	47.1°	42.8°

16. Using the *measured* values in Table 5, plot (by hand) the following figures using the graph paper attached at the end of the report: (1) $|Y|$ versus source frequency; (2) $\angle Y$ versus source frequency; (3) I versus source frequency.

17. For the above plots, state your conclusions under the plot? Also identify the resonant frequency and bandwidth in each plot.

AC Source Frequency (Hz)	$ S $ (mVA)	$\angle S$ (degrees)	P (mW)	Q (mVAR)	PF value	PF lead or lag
	Measured	Measured	Measured	Measured	Measured	Measured
6000	23	-63.8°	10.155	-20.637	0.442	lead
9000	14	-42.7°	10.289	-9.494	0.735	lead
14400	10.4	-12.2°	10.165	-2.198	0.977	lead
16800	12.4	15°	11.977	3.209	0.966	lag
30000	15.6	42.4°	11.52	10.519	0.738	lag
48000	24.8	63°	11.259	22.097	0.454	lag
$f_r = 15915$	12.4	2°	12.392	0.433	0.999	lag
$f_1 = 8936.3$	14	-38°	11.326	-8.619	0.809	lead
$f_2 = 28345.4$	15	42.8°	11.006	10.192	0.734	lag

19. Using the values in Table 6, plot (by hand) the following figure using the graph paper attached at the end of the report: P and Q on the same plot versus source frequency.

20. For the above plot, state your conclusions under the plot?

21. At what frequency the real power P is minimum? Why?

At 6000 Hz due to small power factor.

22. At what frequency the magnitude of the reactive power $|Q|$ is maximum? Why?

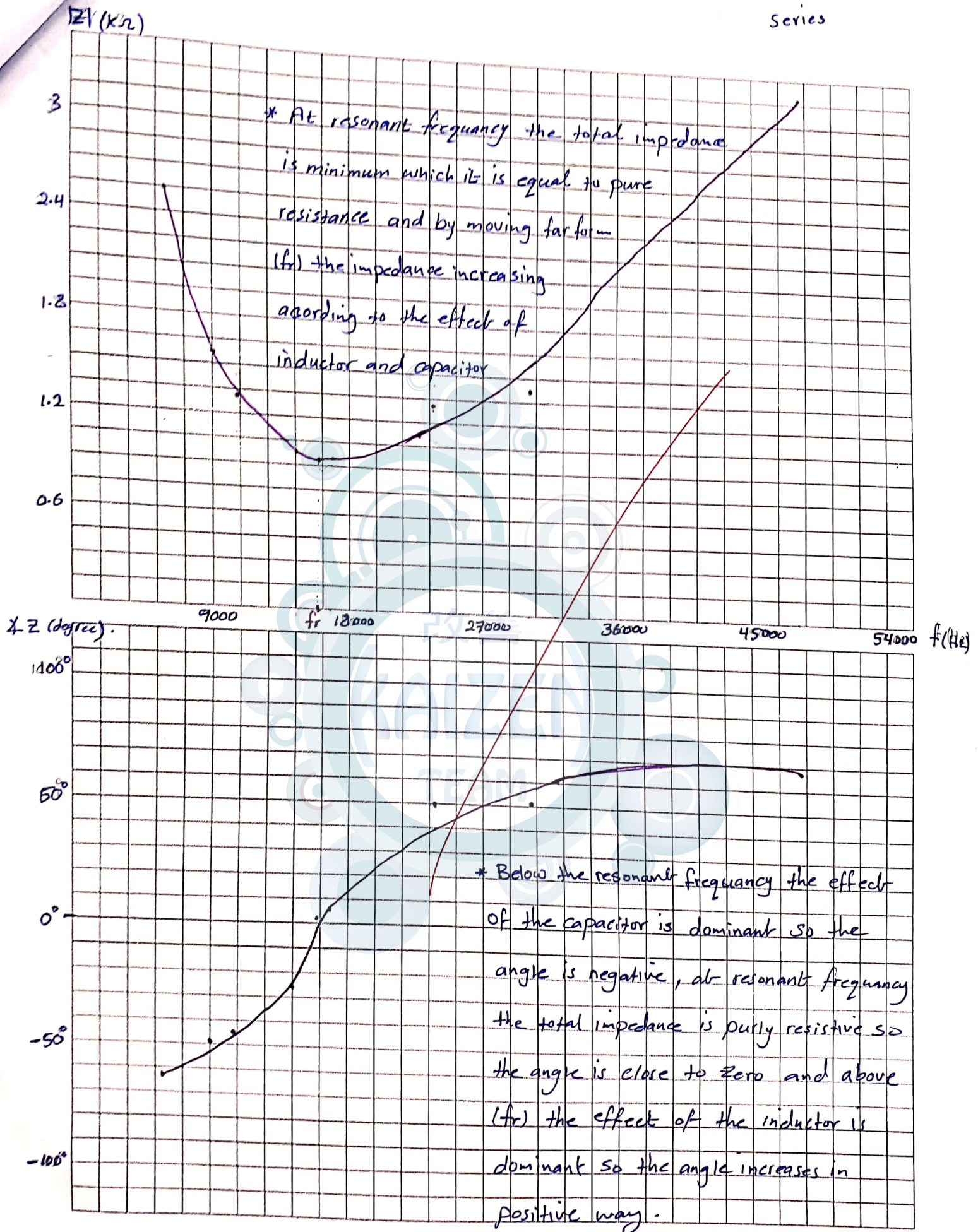
... At 48000 Hz due to small power factor ...

CONCLUSIONS

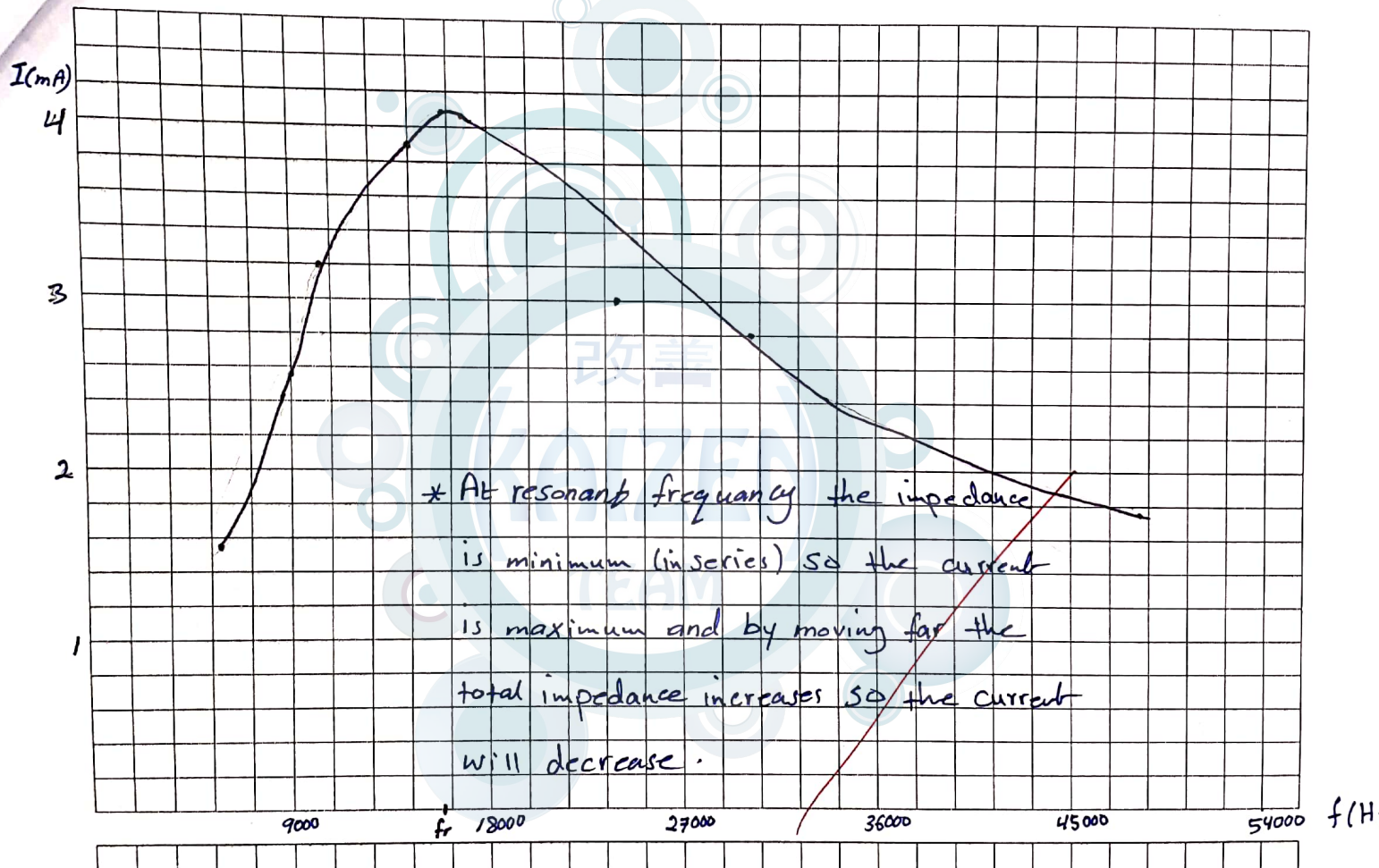
Summarize in clear but concise format what you learned from this experiment:

... This experiment describe the resonant circuit in both configurations: series and parallel, how to ~~connect~~ choose resonant frequency according to the values of resistors, capacitor, inductor and then the relation between changing the frequency and its effect on different values in the circuit such that: Voltage, current, total impedance, total admittance, phase shift, real power and reactive power in parallel and series configurations.

** End **



Series



Parallel.

$\angle Y$ (degree)

75°
60
45
30
15
0
-15°
-30°
-45°
-60°
-75°

* Above the resonant frequency the circuit tend to be capacitive so the angle of total impedance becomes negative and the angle of admittance becomes positive

* Below the resonant frequency the circuit tend to be ~~capacitive~~^{inductive} so the angle of total impedance ~~becomes positive~~^{so} the angle of admittance becomes negative

9000 fr 18000 27000 36000 45000 54000

f (Hz)

Y (degree)

3
2.4
1.8
1.2
0.6

* At resonant frequency the impedance is maximum (in parallel configuration), so the admittance is minimum and increasing be moving far from (fr.)

Parallel

